

Class 11 Relations and Functions Test 4

1. If $f(x) + 2f\left(\frac{1}{x}\right) = 3x, x \neq 0$ and $S = \{x \in \mathbf{R} : f(x) = f(-x)\}$ then
- $n(S) = 2$
 - $n(S) > 2$
 - $n(S) = 1$
 - $S = \phi$
2. Range of the function $f: \mathbf{W} \rightarrow \mathbf{W}, f(x) = x - 5\left[\frac{x}{5}\right]$, where $[x]$ is greater integer function, is
- \mathbf{W}
 - \mathbf{N}
 - $\{1, 2, 3, 4, 5\}$
 - $\{0, 1, 2, 3, 4\}$
3. If $f(x) = \log\left(\frac{1-x}{1+x}\right), |x| < 1$ then $f\left(\frac{2x}{1+x^2}\right)$ is equal to
- $(f(x))^2$
 - $2f(x)$
 - $-2f(x)$
 - $2f(x^2)$
4. For $x \in \mathbf{R} - \{-1, 1\}$, range of the function $f(x) = \frac{x^2}{1-x^2}$ is
- $\mathbf{R} - \{-1\}$
 - $\mathbf{R} - (-1, 0)$
 - $[0, \infty)$
 - $\mathbf{R} - [-1, 0)$
5. Domain of the function $f(x) = \frac{1}{4-x^2} + \log_{10}(x^3 - x)$ is
- $(-1, 0) \cup (1, 2) \cup (2, \infty)$
 - $(1, 2) \cup (2, \infty)$
 - $(-1, 0) \cup (1, 2) \cup (3, \infty)$
 - $(-2, -1) \cup (-1, 0) \cup (2, \infty)$
6. For $x \in \mathbf{R}, [x]$ is greatest integer function then $\left[\frac{-1}{3}\right] + \left[\frac{-1}{3} - \frac{1}{100}\right] + \left[\frac{-1}{3} - \frac{2}{100}\right] + \dots + \left[\frac{-1}{3} - \frac{99}{100}\right]$ is equal to
- -135
 - -131
 - -153
 - -133
7. Range of the function $f: \mathbf{N} \rightarrow \mathbf{N}, f(n) = \begin{cases} \frac{n+1}{2} & \text{when } n \text{ is odd} \\ \frac{n}{2} & \text{when } n \text{ is even} \end{cases}$
- \mathbf{W}
 - \mathbf{N}
 - \mathbf{R}_0
 - \mathbf{Q}
8. Range of the function $f(x) = \frac{x}{1+x^2}$ is
- $\mathbf{R} - [-1, 1]$
 - $(-1, 1) - \{0\}$
 - $\mathbf{R} - \left[\frac{-1}{2}, \frac{1}{2}\right]$
 - $\left[\frac{-1}{2}, \frac{1}{2}\right]$
9. Range of the function $f: \mathbf{R}^+ \rightarrow \mathbf{R}, f(x) = \left\lfloor 1 - \frac{1}{x} \right\rfloor$ is
- $(-\infty, -1)$
 - $(-\infty, 1)$
 - $(1, \infty)$
 - $(0, \infty)$
10. $f(x) = a^x$ is written as $f(x) = f_1(x) + f_2(x)$ where $f_1(x)$ is even function & $f_2(x)$ is odd function then $f_1(0)$ is equal to
- 0
 - 1
 - -1
 - 2

11. Domain of the function

$$f(x) = \frac{1}{\sqrt{|x| - x}}$$

- (a) \mathbf{R}
 (b) \mathbf{R}_0
 (c) \mathbf{R}^+
 (d) \mathbf{R}^-

12. Which of these relations is not a function.

- (a) $R = \left\{ (x, y) : y = \frac{1}{x}, x \in R_0 \right\}$
 (b) $R = \{(x, y) : x = |y|, x, y \in R\}$
 (c) $R = \{(x, y) : |x + y| = 10, x, y \in R^+\}$
 (d) $R = \{(x, y) : x^2 = y^2, x, y < 0\}$

13. The domain of the function
- $f(x) = \frac{1}{\sqrt{x - [x]}}$
- is

- (a) \mathbf{R}^+
 (b) $\mathbf{R} - \mathbf{I}$
 (c) \mathbf{R}_0
 (d) $\mathbf{R}_0 - \mathbf{I}$

14. Find the domain of definition of
- $f(x) = \frac{\log_2(x+3)}{x^2 + 3x + 2}$

- (a) $(-3, \infty)$
 (b) $\{-1, -2\}$
 (c) $(-3, \infty) - \{-1, -2\}$
 (d) $(-\infty, \infty)$

15. The domain of definition of the function
- $y(x)$
- given by
- $2^x + 2^y = 2$
- is

- (a) $(0, 1]$
 (b) $[0, 1]$
 (c) $(-\infty, 0]$
 (d) $(-\infty, 1)$

16. The domain of the function
- $f(x) = \log_{3+x}(x^2 - 1)$
- is

- (a) $(-3, -1) \cup (1, \infty)$
 (b) $[-3, -1) \cup [1, \infty)$
 (c) $(-3, -2) \cup (-2, -1) \cup (1, \infty)$
 (d) $[-3, -2) \cup (-2, -1) \cup [1, \infty)$

17. Range of the function
- $f(x) = \frac{x^2 + x + 2}{x^2 + x + 1}$

- (a) $x \in R$ is
 (b) $(1, \infty)$
 (c) $(1, 11/7)$
 (d) $(1, 7/3]$

18. Domain of
- $f(x) = \sqrt{2\{x\}^2 - 3\{x\} + 1}$
- where
- $\{.\}$
- denotes the fractional part, in
- $[-1, 1]$
- , is

- (a) $[-1, 1] \sim \left(\frac{1}{2}, 1\right)$
 (b) $\left[-1, -\frac{1}{2}\right] \cup \left[0, \frac{1}{2}\right] \cup \{1\}$
 (c) $\left[-1, \frac{1}{2}\right]$
 (d) $\left[-\frac{1}{2}, 1\right]$

19. If
- $f(x) = \text{maximum}\left\{x^3, x^2, \frac{1}{64}\right\} \forall x \in [0, \infty)$
- , then

- (a) $f(x) = \begin{cases} x^2, & 0 \leq x \leq 1 \\ x^3, & x > 1 \end{cases}$
 (b) $f(x) = \begin{cases} \frac{1}{64}, & 0 \leq x \leq \frac{1}{4} \\ x^2, & \frac{1}{4} < x \leq 1 \\ x^3, & x > 1 \end{cases}$
 (c) $f(x) = \begin{cases} \frac{1}{64}, & 0 \leq x \leq \frac{1}{8} \\ x^2, & \frac{1}{8} < x \leq 1 \\ x^3, & x > 1 \end{cases}$
 (d) $f(x) = \begin{cases} \frac{1}{64}, & 0 \leq x \leq \frac{1}{8} \\ x^3, & x > 1/x \end{cases}$

20. If
- x
- satisfies
- $|x - 1| + |x - 2| + |x - 3| \geq 6$
- , then

- (a) $0 \leq x \leq 4$
 (b) $x \leq -2$ or $x \geq 4$
 (c) $x \leq 0$ or $x \geq 4$
 (d) None of these

21. The minimum value of
- $f(x) = |x - 1| + |x - 2| + |x - 3|$
- is equal to.

- (a) 1
 (b) 2
 (c) 3
 (d) Zero

22. $f: \mathbf{R} \rightarrow \mathbf{R}$, where $f(x) = \frac{x^2 + ax + 1}{x^2 + x + 1}$. Complete set of values of 'a' such that range of $f(x)$ is \mathbf{R}
- (a) $(-\infty, \infty)$
 (b) $(-\infty, 0)$
 (c) $(0, \infty)$
 (d) None
23. If f is a function such that $f(0) = 2$, $f(1) = 3$ and $f(x+2) = 2f(x) - f(x+1)$ for every real x then $f(5)$ is
- (a) 7
 (b) 13
 (c) 1
 (d) 5
24. $|x-3| + |x-1| \geq 3$, set of values of x satisfying the equation is
- (a) $[4, \infty)$
 (b) $(-\infty, 0]$
 (c) $(-\infty, \frac{1}{2}] \cup [\frac{7}{2}, \infty)$
 (d) $[\frac{7}{2}, \infty)$
25. Period of the function $|\sin 2x| + |\cos 2x|$ is
- (a) $\frac{\pi}{2}$
 (b) π
 (c) 2π
 (d) $\frac{\pi}{4}$
26. Period of $f(x) = x - [x+a] - b$, where $a, b \in \mathbf{R}$ and $[.]$ denotes the greatest integer function, is
- (a) a
 (b) b
 (c) $|a-b|$
 (d) 1
27. Domain of the function $f(x) = \sqrt{\frac{1}{4} - \sin^2 x}$, $x \in [0, \pi]$, is
- (a) $[\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}]$
 (b) $[\frac{\pi}{4}, \frac{3\pi}{4}]$
 (c) $[0, \frac{\pi}{4}] \cup [\frac{3\pi}{4}, \pi]$
 (d) none of these
28. If $\{x\} = [x]$ then number of solutions of the equation is
- (a) 2
 (b) 3
 (c) 1
 (d) more than 2
29. Domain of the function $f(x) = \frac{2x-1}{x-3}$ for $x \geq 4$ is
- (a) $[2, 7]$
 (b) $(2, 7]$
 (c) \mathbf{R}
 (d) $\mathbf{R} - \{2\}$
30. Which of the functions is odd
- (a) $f(x) = x^{100} + 1$
 (b) $f(x) = e^x + e^{-x}$
 (c) $f(x) = \frac{1}{|x|}$
 (d) None of the above